

Orthogonal rational functions on the unit circle: theory, applications and generalizations*

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Abstract

We give a survey of the basic theory of orthogonal rational functions with poles outside the unit disk. We give a motivation by linear prediction and signal processing applications. We include the basic theory of recurrence relations, Christoffel-Darboux relations, reproducing kernels, associated functions and interpolation properties, para-orthogonal functions and quadrature, moment problems and Favard theorems, and convergence properties.

We touch only briefly on the following related and generalized topics. We give an indication of related results for the case where the poles (interpolation points) are on the boundary (i.e. the circle). We briefly consider the case where the functions are matrix valued and relate it to tangential interpolation problems. Some results are mentioned for the case where the inner product is taken w.r.t. a Gramm matrix which is quasi Toeplitz and finally we mention related results about time-varying systems.

1 Motivation (linear prediction)

Let $s = (s_n) \in \ell_2$ be a discrete signal. Its Fourier transform $S(e^{i\omega}) \in L_2$ is called its *spectrum*, while we call $R(e^{i\omega}) = |S(e^{i\omega})|^2$ the *power spectrum*. Defining $S_*(z) = \overline{S(1/\bar{z})}$, we can write this as $R(t) = S(t)S_*(t)$ with $t \in \mathbb{T} = \{z \in \mathbb{C} : |z| = 1\}$. When $R(z) = \sum_k r_k z^k$, then we call the sequence $r = (r_k)$ the *autocorrelation function* of the signal s . Obviously $r_n = \sum_k s_{n+k} \bar{s}_k = \overline{r_{-k}}$, $n \in \mathbb{Z}$. The *energy* of the signal corresponds to $r_0 = \|s\|^2 = \|S\|^2$. In the linear prediction problem, we want to predict the value of s_n from its past, i.e., by the estimate $\hat{s}_n = -\sum_{k \geq 1} a_k s_{n-k}$. Assume that the signal is in a stationary regime, so that the a_k do not depend on n . The corresponding prediction error is $e_n = s_n - \hat{s}_n = \sum_{k \geq 0} a_k s_{n-k}$ or in the frequency domain: $E(z) = A(z)S(z)$, with $a_0 = A(0) = 1$. The best possible such a model in least squares sense is the one which minimizes $\|e\|^2 = \|E\|^2 = \|AS\|^2 = \|A\|_k^2$

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Orthogonal Rational Functions

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Table of Contents Orthogonal Rational Functions

1. Understanding the eBook Orthogonal Rational Functions
 - The Rise of Digital Reading Orthogonal Rational Functions
 - Advantages of eBooks Over Traditional Books
2. Identifying Orthogonal Rational Functions
 - Exploring Different Genres
 - Considering Fiction vs. Non-Fiction
 - Determining Your Reading Goals
3. Choosing the Right eBook Platform
 - Popular eBook Platforms
 - Features to Look for in an Orthogonal Rational Functions
 - User-Friendly Interface
4. Exploring eBook Recommendations from Orthogonal Rational Functions
 - Personalized Recommendations
 - Orthogonal Rational Functions User Reviews and Ratings
 - Orthogonal Rational Functions and Bestseller Lists
5. Accessing Orthogonal Rational Functions Free and Paid eBooks
 - Orthogonal Rational Functions Public Domain eBooks
 - Orthogonal Rational Functions eBook Subscription Services
 - Orthogonal Rational Functions Budget-Friendly Options
6. Navigating Orthogonal Rational Functions eBook Formats
 - ePub, PDF, MOBI, and More
 - Orthogonal Rational Functions Compatibility with Devices
 - Orthogonal Rational Functions Enhanced eBook Features
7. Enhancing Your Reading Experience
 - Adjustable Fonts and Text Sizes of Orthogonal Rational Functions
 - Highlighting and Note-Taking Orthogonal Rational Functions
 - Interactive Elements Orthogonal Rational Functions

8. Staying Engaged with Orthogonal Rational Functions
 - Joining Online Reading Communities
 - Participating in Virtual Book Clubs
 - Following Authors and Publishers Orthogonal Rational Functions
9. Balancing eBooks and Physical Books Orthogonal Rational Functions
 - Benefits of a Digital Library
 - Creating a Diverse Reading Collection Orthogonal Rational Functions
10. Overcoming Reading Challenges
 - Dealing with Digital Eye Strain
 - Minimizing Distractions
 - Managing Screen Time
11. Cultivating a Reading Routine Orthogonal Rational Functions
 - Setting Reading Goals Orthogonal Rational Functions
 - Carving Out Dedicated Reading Time
12. Sourcing Reliable Information of Orthogonal Rational Functions
 - Fact-Checking eBook Content of Orthogonal Rational Functions
 - Distinguishing Credible Sources
13. Promoting Lifelong Learning
 - Utilizing eBooks for Skill Development
 - Exploring Educational eBooks
14. Embracing eBook Trends
 - Integration of Multimedia Elements
 - Interactive and Gamified eBooks

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