

# NUMERICAL METHODS

C / KAPPA EXAM 12 / 11/19 / 2022 [20.000]

## LEAST SQUARES REGRESSION

Goal: minimize the sum of the squares of the residual errors.



$$S_r = \sum_{i=1}^n d_i = \sum_{i=1}^n (y_i - a_0 - a_1 x_i)$$

1. sum of the square errors.  
2. minimize the square of the errors.

$$a_0 = \frac{\sum y_i - a_1 \sum x_i}{n}$$

$$a_0 = \frac{\sum y_i}{n} \quad a_1 = \frac{\sum x_i y_i}{\sum x_i^2}$$

## STANDARD ERROR:

$$S_{y_1} = \sqrt{\frac{\sum y_i^2}{n-2}} \quad S_{y_2} = \sqrt{\frac{\sum (y_i - \hat{y}_i)^2}{n-2}}$$

## STANDARD DEVIATION:

$$S_y = \sqrt{\frac{\sum y_i^2}{n-1}} \quad S_x = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}}$$

$$a_0 = \bar{y} - a_1 \bar{x}$$

## INTERPOLATION

Use a polynomial fit:



$$P_n(x) = a_0 + a_1 x + a_2 x^2 + \dots + a_n x^n$$



### SPINES:

$$P_n = \frac{f(x_{i-1}) - f(x_i)}{x_{i-1} - x_i}$$

## POLYNOMIAL QUADRATIC REGRESSION:



$$S_r = \sum_{i=1}^n (y_i - a_0 - a_1 x_i - a_2 x_i^2)^2$$

Take derivative of  $S_r$  to find minimum.

$$\frac{\partial S_r}{\partial a_0} = -2(\sum y_i - \sum a_0 - a_1 \sum x_i - a_2 \sum x_i^2) = 0$$

$$\frac{\partial S_r}{\partial a_1} = -2(\sum y_i x_i - \sum a_0 \sum x_i - a_1 \sum x_i^2 - a_2 \sum x_i^3) = 0$$

$$\frac{\partial S_r}{\partial a_2} = -2(\sum y_i x_i^2 - \sum a_0 \sum x_i^2 - a_1 \sum x_i^3 - a_2 \sum x_i^4) = 0$$

$$\begin{bmatrix} \sum 1 & \sum x_i & \sum x_i^2 \\ \sum x_i & \sum x_i^2 & \sum x_i^3 \\ \sum x_i^2 & \sum x_i^3 & \sum x_i^4 \end{bmatrix} \begin{bmatrix} a_0 \\ a_1 \\ a_2 \end{bmatrix} = \begin{bmatrix} \sum y_i \\ \sum y_i x_i \\ \sum y_i x_i^2 \end{bmatrix}$$

Matrix  $A$  is invertible.  $C = \begin{bmatrix} \sum y_i \\ \sum y_i x_i \\ \sum y_i x_i^2 \end{bmatrix}$ .  $X = \begin{bmatrix} a_0 \\ a_1 \\ a_2 \end{bmatrix}$ .  $A^{-1} C = X$ .  
Coefficients of determination:  $R^2 = \frac{S_r - S_{min}}{S_r}$

## ODE'S

### Euler's Method

$$\frac{dy}{dx} = f(x,y) \quad y_{i+1} = y_i + f(x_i, y_i) \Delta x$$

### Runge-Kutta Method

$$\frac{dy}{dx} = f(x,y)$$

$$y' = \frac{y^2 + 2x}{2} = f(x,y)$$

$$y' = \frac{y^2 + 2x}{2} = f(x_i, y_i) + f(x_{i+1}, y_{i+1})$$

Taylor Series:  
 $y(x+\Delta x) = y(x) + \Delta x y'(x) + \frac{\Delta x^2}{2} y''(x) + \dots$   
 $y(x+\Delta x) = y(x) + f(x,y) \Delta x$

### Classic 4th order Runge-Kutta

$$y_{i+1} = y_i + \frac{\Delta x}{4} (k_1 + 2k_2 + 2k_3 + k_4)$$

$$k_1 = f(x_i, y_i)$$

$$k_2 = f(x_i + \frac{1}{2} \Delta x, y_i + \frac{1}{2} \Delta x k_1)$$

$$k_3 = f(x_i + \frac{1}{2} \Delta x, y_i + \Delta x k_2)$$

$$k_4 = f(x_i + \Delta x, y_i + \Delta x k_3)$$

## PDE'S

### Finite Difference Method



## EIGEN VALUES

$\lambda = \text{Eigen Value}$

Example:

$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

Single 2x2:

$$A = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$A - \lambda I = \begin{bmatrix} a-\lambda & b \\ c & d-\lambda \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$\lambda = \frac{a+d}{2} \pm \sqrt{\left(\frac{a-d}{2}\right)^2 + bc}$$

Two eigen values with same eigenvector:

$$\begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$x_1 + x_2 = 0 \Rightarrow x_1 = -x_2$$

$$x_1 + x_2 = 0 \Rightarrow x_1 = -x_2$$

Two eigen values with different eigenvectors:

$$\begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$-x_1 + x_2 = 0 \Rightarrow x_1 = x_2$$

$$x_1 + -1x_2 = 0 \Rightarrow x_1 = x_2$$

**1D Heat Conduction**

1D Rod of length L, cross-section A, thermal conductivity k.

Boundary conditions:  $T = T_1$  at  $x=0$ ,  $T = T_2$  at  $x=L$ .

Central Difference:

$$u_{i+1}(t) = u_i(t) - \alpha \Delta x (u_{i+1}(t) - u_{i-1}(t)) + \alpha \Delta x^2 u_{xx}(t)$$

$$u_{i+1}(t) = u_i(t) + \alpha \Delta x (u_{i+1}(t) - u_{i-1}(t)) + \alpha \Delta x^2 u_{xx}(t)$$

**2D Heat Conduction**

2D Plate of length L, width W, thermal conductivity k.

Boundary conditions:  $T = T_1$  at  $x=0$ ,  $T = T_2$  at  $x=L$ ,  $T = T_3$  at  $y=0$ ,  $T = T_4$  at  $y=W$ .

Central Difference:

$$u_{i,j}(t) = \frac{1}{4} (u_{i+1,j}(t) + u_{i-1,j}(t) + u_{i,j+1}(t) + u_{i,j-1}(t)) + \alpha \Delta x^2 \Delta y^2 u_{xx}(t)$$

**5th Rank of a Matrix**

Local's finite diff adjacent to boundary:

$$\begin{bmatrix} 0 & -1 & 0 & -1 & 0 & -1 & 0 & -1 & 0 \end{bmatrix} u = 0$$

**RIGHT BOUNDARY B.C.**

$$\frac{\partial u}{\partial x} = 0 = \frac{u_{i+1,j} - u_{i-1,j}}{2\Delta x}$$

$$u_{i+1,j} = u_{i-1,j} + 2\Delta x u_{xx}$$

**[A] MATRIX:**

Centered finite-diff 2D heat conduction:

$$f_{i,j} = \frac{f_{i+1,j} - f_{i-1,j}}{2\Delta x}$$

$$f_{i,j} = \frac{f_{i,j+1} - f_{i,j-1}}{2\Delta y}$$

**FINITE DIFFS:**

Centered finite-diff 2D heat conduction:

$$f_{i,j} = \frac{f_{i+1,j} - f_{i-1,j}}{2\Delta x}$$

$$f_{i,j} = \frac{f_{i,j+1} - f_{i,j-1}}{2\Delta y}$$

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**Daniela Niemeyer**



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